1. Details of Module and its structure

Module Detail	
Subject Name	Physics
Course Name	Physics 04 (Physics Part-2, Class XII)
Module Name/Title	Unit-06, Module-10: Wave Optics Chapter-10: Wave Optics
Module Id	leph_201001_eContent
Pre-requisites	Incident ray, reflected ray, laws of refection and refraction, Snell's law, Angle of incidence , Angle of reflection, Angle of refraction
Objectives	After going through this lesson, the learners will be able to • Distinguish between Ray and Wavefront • Understand the Huygens' principle • Distinguish between the spherical, cylindrical and plane wavefront. • Understand the shape of wave fronts after reflection and refraction through mirrors, lenses and prism. • Apply the Huygens' Principle to explain laws of reflection and refraction
Keywords	Wave front, Ray, spherical wave front, plane wave front, Huygens's construction

2. Development Team

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1. UNIT SYLLABUS

UNIT 6: Optics

Chapter–9: Ray Optics and Optical Instruments

Ray optics: Reflection of light; spherical mirrors; mirror formula; refraction of light; total internal reflection and its applications; optical; fibers; refraction at spherical surfaces; lenses; thin lens formula; lens maker's formula; magnification, power of a lens; combination of thin lenses in contact; refraction and dispersion of light through a prism.

Scattering of light – blue color of sky and reddish appearance of the sun at sunrise and sunset

Optical instruments – microscopes and astronomical telescopes (refracting and reflecting) and their magnifying powers

Chapter-10: Wave Optics

Wave optics: Wave front and Huygens's principle, reflection and refraction of plane wave at a plane surface using wave fronts. proof of laws of reflection and refraction using Huygens's principle. Interference, Young's double slit experiment and expression for fringe width, coherent sources and sustained interference of light; diffraction due to a single slit width of central maximum; resolving power of microscope and astronomical telescope. Polarisation, plane polarised light, Malus's law, Brewster's law, uses of plane polarised light and polaroid.

2. MODULEWISE DISTRIBUTION OF UNIT SYLLABUS 15 MODULES

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	• Light falling on surfaces of any shape texture • Peculiar observations
Module 2	• Reflection of light • Laws of reflection • Reflection of light by plane and spherical surfaces • Spherical Mirrors aperture, radius of curvature, pole principal axis • Focus, Focal length, focal plane • Image – real and virtual • Sign convention • The mirror equation, magnification • To find the value of image distance v for different values of object distance u and find the focal length of a concave mirror • Application of mirror formula
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Module 4	• Special effects due to refraction • Real and apparent depth • To determine the refractive index of liquid using a travelling microscope • Total internal reflection • Optical fibers and other applications
Module 5	• Refraction through a prism • Deviation of light -angle of deviation • Angle of minimum deviation • Expression relating refractive index for material of the prism and angle of minimum deviation

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Module 6	• Refraction at spherical surfaces • Radius of curvature • Refraction by a lens • Foci, focal plane, focal length, optical center, principal axis • Formation of images real and virtual • Lens maker's formula • Lens formula and magnification • Sign convention • Application of lens formula • Power of lens • Combination of thin lenses in contact
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Module 15	• **Polarisation** • **to observe polarization of light using two polaroid** • **Plane polarised light** • **Polariser analyser Malus law** • **Brewster/s law** • **Polarisation due to scattering** • **Uses of plane polarised light and polaroids**

Module 10

3. WORDS YOU MUST KNOW

Let us remember the words we have been using in our study of this physics course.

Incident ray: path of light from a source in any preferred direction of propagation

Reflected ray: path of light bounced off from a surface at the point of incidence

Refracted ray: path of light when it propagates from one transparent medium to another.

Normal at the point of incidence: normal to the surface at the point of incidence. Important when the surface is spherical or uneven

Converging and diverging rays: rays of light may converge to or seem to diverge from a point after reflection or refraction such rays are called converging or diverging rays.

Laws of reflection: Laws followed by light rays whenever they interact with a surface

- The incident ray, reflected ray and the normal ,at the point of incidence, lie in the same plane
- The angle of reflection is equal to the angle of incidence

Snell's law: For oblique incidence of light on a transparent medium surface

$$\text{refractive index} = \frac{\sin \text{i}}{\sin \text{r}}$$

- The incident ray, refracted ray and the normal at the point of incidence all lie in the same plane
- The angle of refraction is not equal to the angle of incidence.
- A ray of light propagating from a rarer to a denser medium moves towards the normal. This can be observed for obliquely incident rays.

Plane mirror: a polished surface with infinite radius of curvature

Spherical mirror- concave and convex: spherical mirrors are part of spherical surfaces. The polished surface makes them concave or convex.

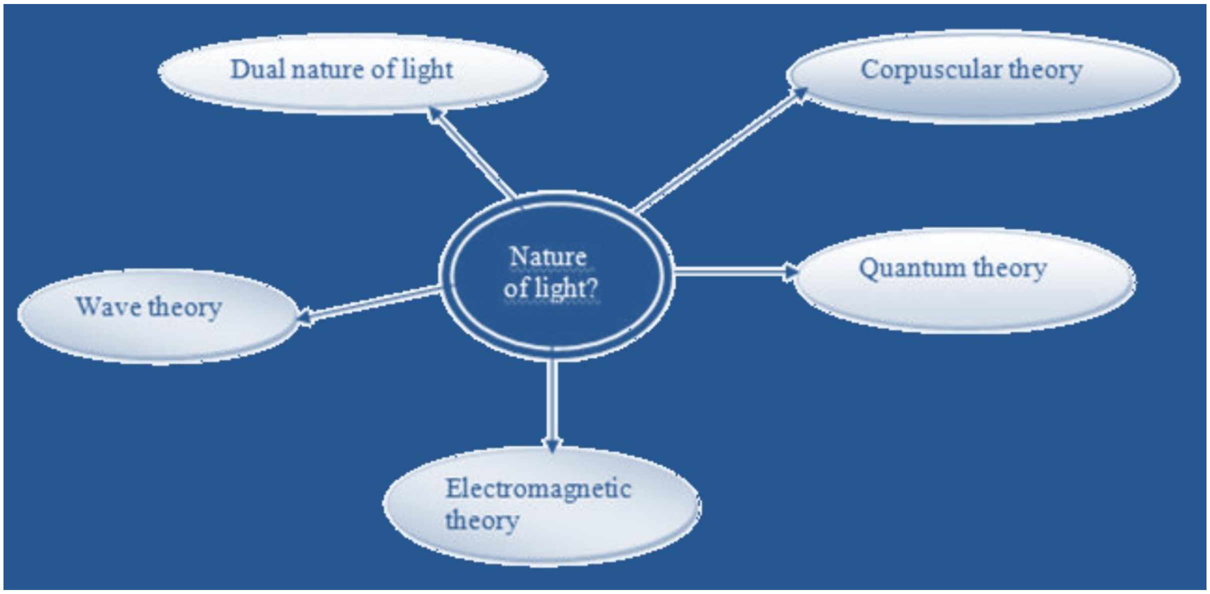
Spherical lens-convex and concave: transparent medium bounded by spherical surfaces, if a thin block of medium has two surfaces bulge out, they form a convex lens

Prism: a rectangular block cut along its diagonal gives two prisms. each piece has two refracting surfaces, a base and the angle between the refracting surfaces (in this case $=90^0$) is called angle of prism.

Light Wave: Light is the part of the electromagnetic spectrum. They are transverse waves. light is an electromagnetic wave, produced by transitions of electrons inside the atoms. The frequency depends upon the source atoms. Wavelength depends upon both the source and the medium in which light is travelling.

4. INTRODUCTION

There have been conflicting opinions regarding the nature of light in the history of scientific investigation. Various theories on the nature of light had been put forward by many scientists at different times but **none** by itself could explain all the properties satisfactorily



Let us briefly describe some of these theories.

In **1637,** Descartes gave the corpuscular model of light and used it to derive Snell's law. His model could explain the laws of reflection and refraction of light at an interface.

The corpuscular model predicted that if the ray of light (on refraction) bends towards the normal then the speed of light would be greater in the second medium. This corpuscular model of light was further developed by Isaac Newton in his famous book entitled **OPTICKS.**

In **1678**, the Dutch physicist Christiaan Huygens put forward the wave theory of light. The wave model could satisfactorily explain the phenomena of reflection and refraction; however, it predicted that on refraction if the wave bends towards the normal, the speed of light would be less in the second medium. This was in contradiction to the prediction made by using the corpuscular model of light.

It was (much) later confirmed by experiments carried out by Foucault that the speed of light in water is less than the speed in air confirming the prediction of the wave model.

The wave theory was not readily accepted primarily because of Newton's authority and also because light could travel through vacuum and it was felt that a wave would always requires a medium to propagate from one point to the other.

However, when Thomas Young performed his famous interference experiment in **1801**, it was firmly established **that light is indeed a wave phenomenon**.

After the interference experiment of Young in 1801, for the next 40 years or so, many experiments were carried out involving the interference and diffraction of light waves; these experiments could only be satisfactorily explained by assuming a wave model of light.

Thus, around **the middle of the nineteenth century**, the wave theory seemed to be very well established.

Christian Huygens proposed that light energy propagates from one-point to the other in the form of a wave motion.

He assumed the presence of medium called ether as the medium for propagation of light.

The wave theory explained **Reflection, Refraction, Interference and Diffraction** but could not explain **polarization,** because light waves were assumed to be longitudinal.

This difficulty was overcome by **Fresnel** who assumed light waves to be transverse in nature but the drawback of his theory was his assumption that the ether was a solid elastic medium. Since the speed of light waves was large, the elasticity of the ether should be large, which was a strange property possessed by a practically unobservable medium.

Later on **Michelson-Morley's** experiment disproved the existence of ether.

When the mathematical description of the light as an **electromagnetic wave** was published by **James clerk Maxwell** in **1864**, it was thought that a final understanding on the wave nature of light had been reached.

But the **Photoelectric effect and Compton Effect** demanded a revisit to a particle -like nature of light. **Einstein** interpreted it in terms of the **quantum theory**.

The present stand therefore, is to accept, that light is **dualistic in nature, meaning light behaves both as waves and particles** .

Ray Optics accounts for **macroscopic phenomenon** like **Reflection, Refraction** etc, and deals with interaction of a light beam with surfaces and mediums

Microscopic phenomena like **Interference, Diffraction and Polarization** could be explained on the basis of **wave theory**.

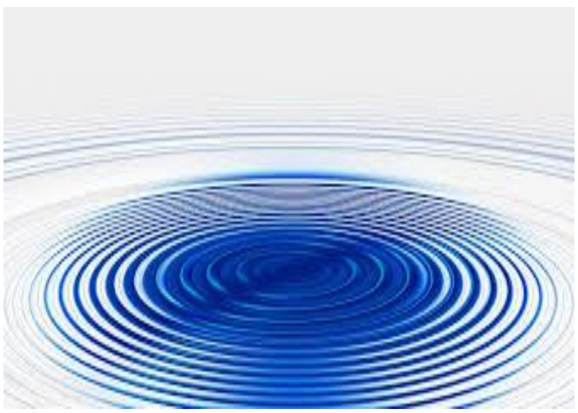
The laws of reflection and refraction; some basic examples of both; some basic ideas about how they relate to the wave nature of light.
https://www.youtube.com/watch?v=nOS0TGeuLoc

Modules 10-15 deal with various phenomena related to wave nature of light

5. WAVEFRONT

Consider dropping a small stone on a calm pool of water. Waves spread out from the point of impact. Every point on the surface starts oscillating one by one. At any instant, a photograph of the surface would show circular rings on which the disturbance is maximum.
You might have seen these circles, when you gently disturb a still water surface, (pond, river water, bucket of water)

Ripples on the surface of water
https://pixabay.com/en/wave-concentric-waves-circles-water-64170/



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We can see concentric circular rings or ripples on the surface of the water which grow as the disturbance travels. The circular rings on the water surface are points where the particles of the water have constant or zero phase difference.

Similarly, if we consider a light source, placed in a homogeneous medium, the velocity of light waves in all directions is the same.

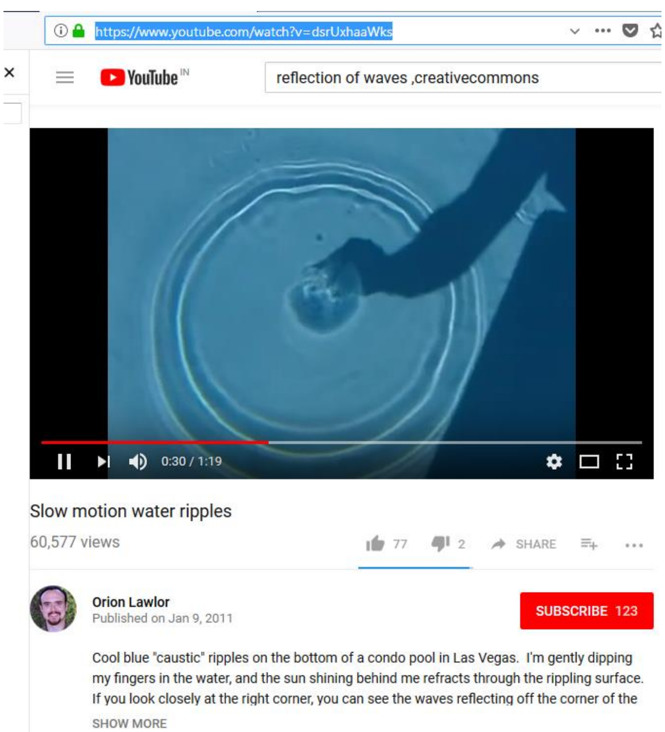
Therefore, the disturbance reaches all points, which are at the same distance from the source, at the same time.

Clearly, **all points on such a surface are oscillating in phase because they are at the same distance from the source.**

It is defined as the locus of points having a zero or constant phase difference.

Such a locus of points, which oscillate in same phase, is called a **WAVEFRONT**;
Thus *a* **wavefront** *is* **defined as a surface of constant phase**.

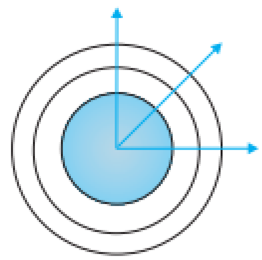
https://www.youtube.com/watch?v=dsrUxhaaWks



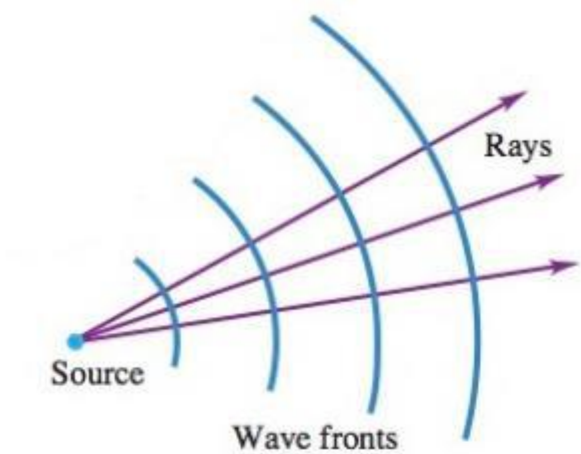
The speed with which the wavefront moves outwards from the source is called the speed of the wave.

The energy of the wave propagates in a direction perpendicular to the wave front. Such directions of energy flow, which are always perpendicular to the wave front, are called rays.

If we have a point source emitting waves uniformly in all directions, then the locus of points which have the same amplitude and vibrate in the same phase are spheres and we have what are known as a ***spherical wavefront*** as shown in figure



A diverging spherical wave emanating from a point source. The wave fronts are spherical



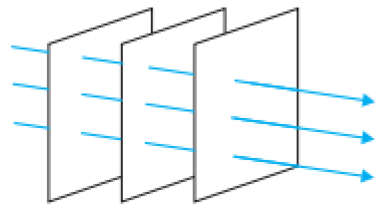
Or

When if it is an extended (light slit) source, with more dimensions in length, the wave front is cylindrical in nature and are called **cylindrical wavefront**

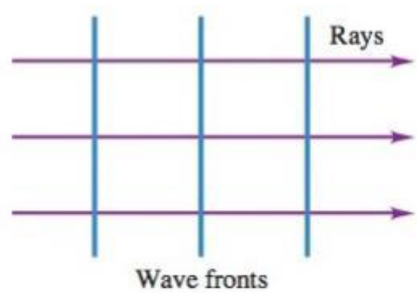
If we look at a small portion of a spherical wave front, very far away from the source, then the part of spherical wave front would look like parallel planes.
The corresponding rays are parallel lines perpendicular to these planes as shown in figure.

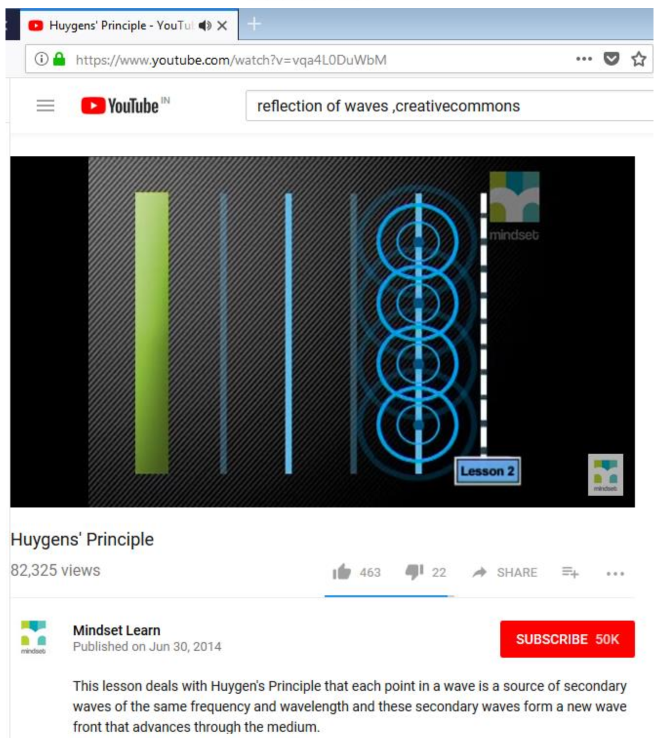
These planes are called **plane wavefront**.

A linear source such as an illuminated slit give rise to **cylindrical wave fronts**. Again at very far distances a portion of these wave fronts can be regarded as plane wave fronts.



Plane wave front is a cross section of a cylindrical wave front in a plane; a cross section of spherical wave front are concentric circles



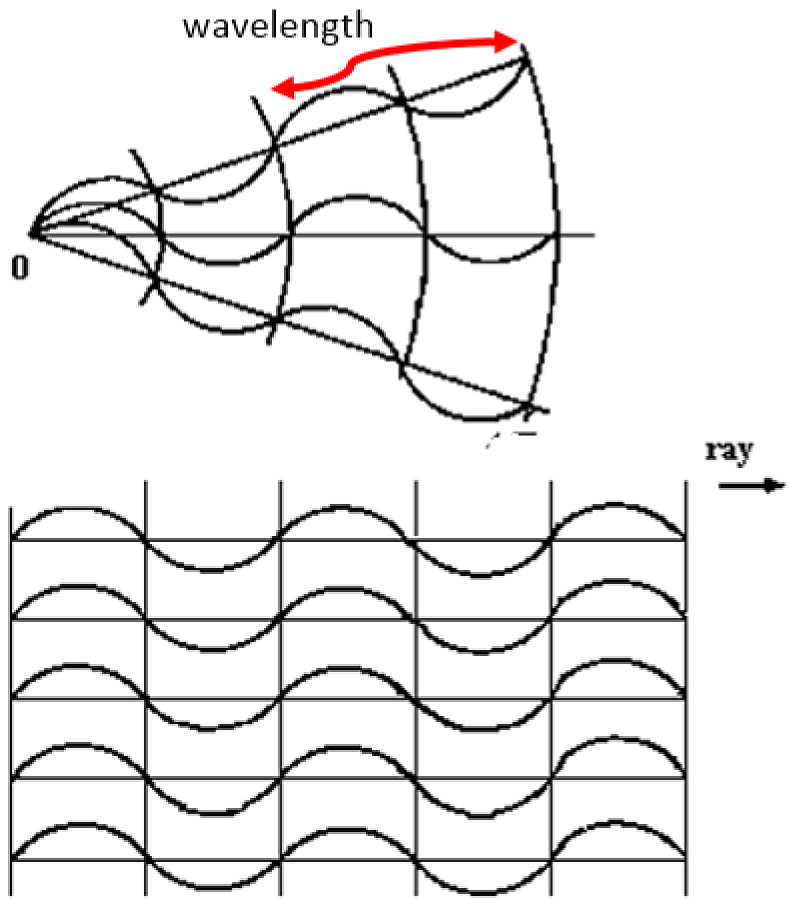


https://www.youtube.com/watch?v=vqa4L0DuWbM

The light waves emerging from a point source, always form a spherical wave front in **homogeneous 3D space** as shown in the figure

You may understand it better by considering the wave and parts of concentric circles showing particles in the same phase.

Here **alternate lines /circles** are in the same phase. Consecutive wave fronts are one wavelength apart.



Notice the **alternate lines /circles** are in the same phase, forming the wavefront, each wavefront is one **wavelength** apart**.**

6. HUYGEN'S PRINCIPLE

Christian Huygens, a Dutch, in 1678, proposed a method to predict new wave front from existing wavefront, as the wave propagated in any direction.

Now, if we know the shape of the wave front at an instant $t = 0$,

Huygens principle allows us to determine the shape of the wave front at a later time τ.

Thus, **Huygens principle is a pure geometrical construction, which, given the shape of the wave front at any time t = 0, allows us to determine the shape of the wave front at a later time.** τ.

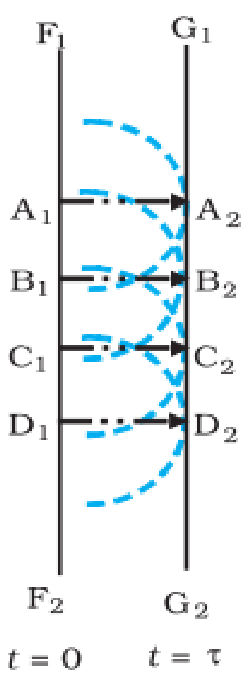
Also Huygens's proposal gives the position and shape of a wave front at any time from its initial position in the same, or in any other medium.

According to **Huygens Principle**:

- **Each point of the wave front is a source of a secondary disturbance and the wavelets emanating from these points spread out in all directions with the speed of the wave. These wavelets emanating from the wave front are usually referred to as secondary wavelets**
- **If we draw a common tangent (in the forward direction) to all these spheres, we obtain the new position of the wave front at a later time.**

Hence **common tangent in the forward direction drawn to all the secondary wavelets give the position and shape of the new wave front. This new wavefront is called secondary wave front.**

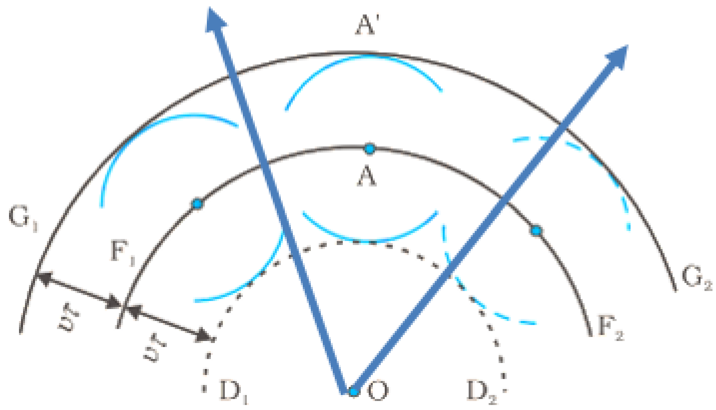
Suppose the light energy travels outwards along straight lines emerging from the source, i.e. radii of spherical wave front.



Huygens geometrical construction for a plane wave propagating to the right. F_1 F_2 is the plane wave front at t = 0 and G_1 G_2 is the wave front at a later time τ.

The lines A_1, A_2, B_1 B_2 … etc. are normal to both F_1 F_2 and G_1 G_2 and represent rays

The blue dotted lines represent spherical wavelets reaching G_1 G_2 at the same instant.

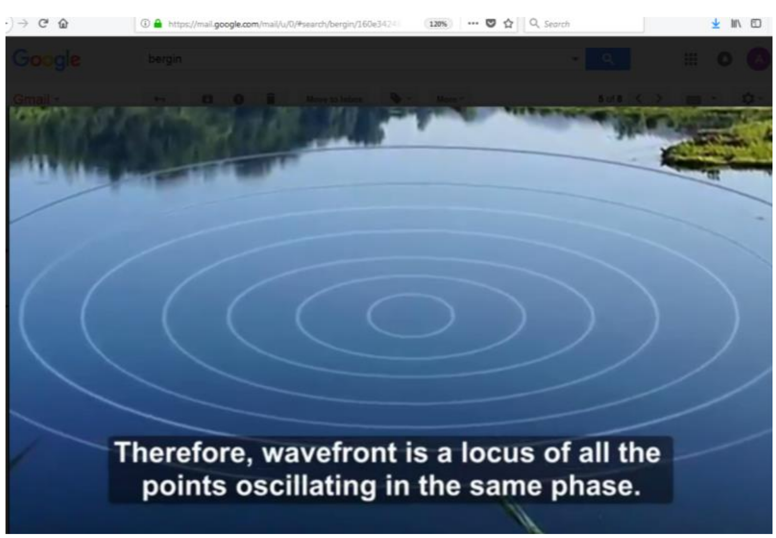


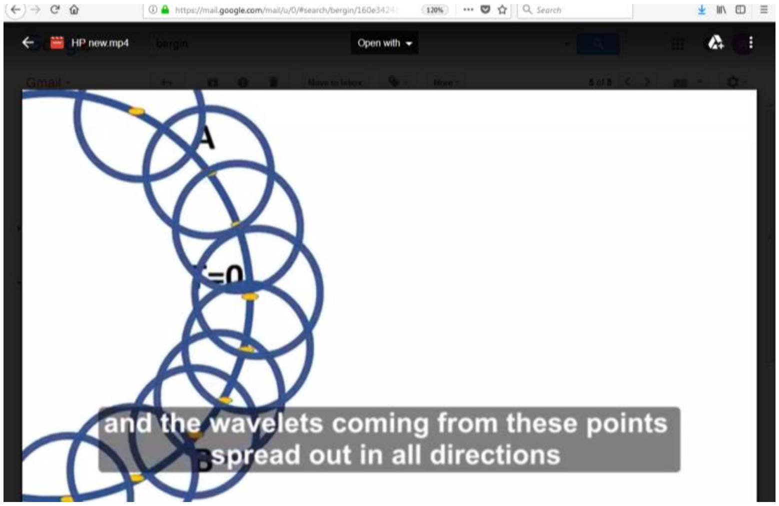
F_1 F_2 represents the spherical wave front (with O as center) at t = 0.
The envelope of the secondary wavelets emanating from F_1 F_2 produces the forward moving wave front G_1 G_2. The back wave D_1D_2 is supposed not to exist.

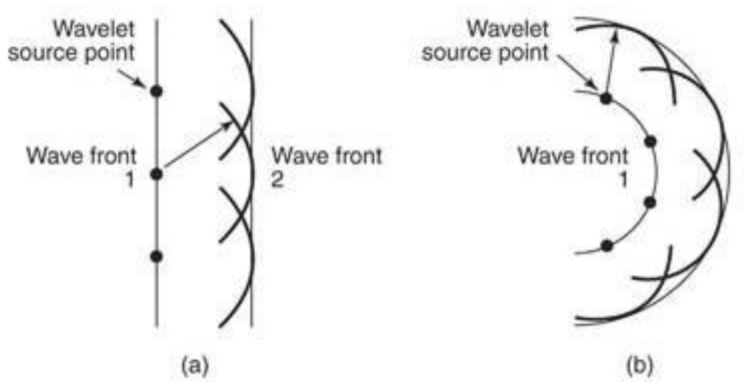
Note

- **The tangent to the blue dotted circles, as proposed by Huygens is the new wave front G_1 G_2**
- **The envelop, which would exist in all directions in 3 D space is ignored and only the envelop in the forward direction of the ray are selected.**
- **So if O is the source the bold lines show the rays**
- **D_1 D_2 is the ignored wave front and**
- **G_1 G_2 the forward envelop is the new wave front.**
- **the construction helps us understand several phenomenon Reflection Refraction Interference and Diffraction**

Watch animation







http://www.cliffsnotes.com/sciences/physics/light/wave-optics

We can thus conclude that-

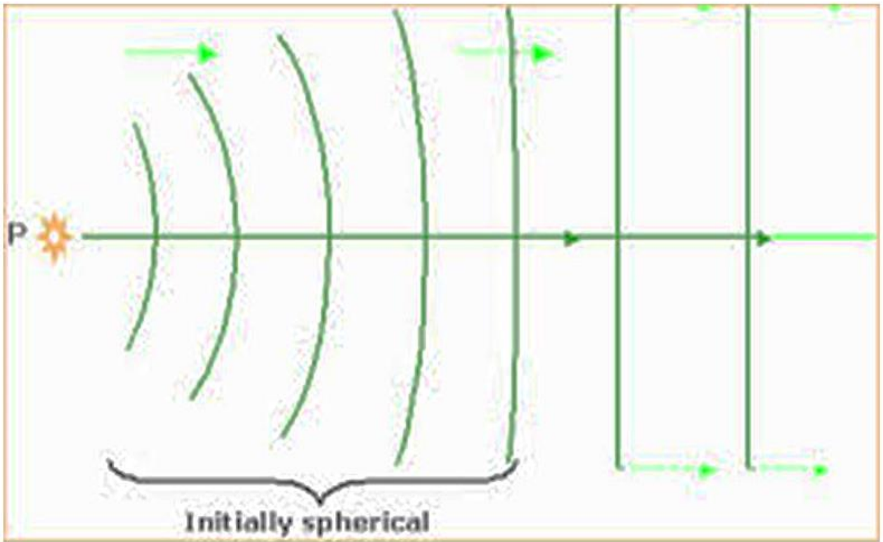
- **The spacing between a pair of wave fronts is constant along any ray, and it is equal to one wavelength between consecutive wavefront**
- **Rays are perpendicular to wave fronts.**
- **The time taken for light waves to travel from one wave front to another wave front is same for any ray.**

EXAMPLE

What is the shape of the wave front in each of the following cases?
(a) Light diverging from a point source.
(b) The portion of the wave front of light from a distant star intercepted by the Earth

SOLUTION

(a) Spherical wavefront
(b) Plane wavefront



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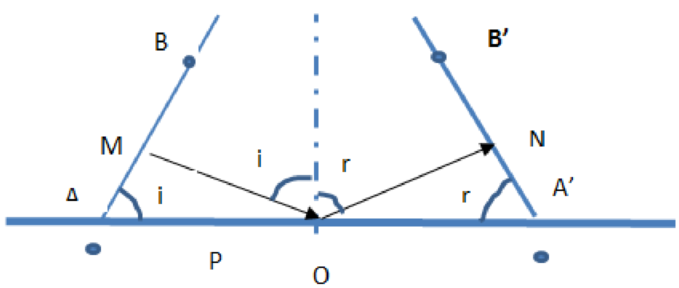
7. REFLECTION OF A PLANE WAVE BY A PLANE SURFACE

Using Huygens's principle explaining Reflection of a plane wave at plane surface which means, considering the wave nature of light to explain the phenomenon of reflection

Now we will able to use Huygens's principle to understand the laws of reflection of light.

Consider an incident plane wave front AB incident at an angle *i* on a reflecting surface P. We can see that when the point A on the incident wave front strikes the surface, the point B still has to move through a distance BA'.



If *v* represents the speed of the wave in the medium and if **τ** represents the time taken by the wave front to advance from the point B to *A'*

then the distance BA' = $v\,\tau$

By this time τ, the secondary wave front of radius $v\,\tau$ with A as center, would have travelled forward whereas the secondary wave front, with A' as center, would have just started i.e. would have zero radius.

In order to the construct the reflected wave front we draw a sphere of radius $v\,\tau$ from the point A as shown in Figure.

Let A'B' represent the tangent plane drawn from the point A' to this sphere.

This secondary wave front from A represent the reflected wave front making an angle r with reflecting surface P.

This angle r is called angle of reflection.

Let us try and prove the laws of reflection

The angle of incidence (i) and angle of reflection (r) are the angles made by the incident and reflected rays respectively, with the normal. These are also the angles between the wave fronts and the surface as shown in the figure.

The time taken by the ray to travel from M to N after striking the surface at O

Total time from M to N = t = $\frac{\mathrm{MO}}{\mathrm{v}} + \frac{\mathrm{ON}}{\mathrm{v}}$

where v is the velocity of the wave.

$$\mathrm{t} = \frac{\mathrm{OA}\sin \mathrm{i}}{\mathrm{v}} + \frac{\mathrm{OB}\sin \mathrm{r}}{\mathrm{v}}$$

or

$$\mathrm{t} = \frac{\mathrm{OA}\sin \mathrm{i}}{\mathrm{v}} + \frac{(\mathrm{AB} - \mathrm{OA})\sin r}{\mathrm{v}}$$

or

$$\mathrm{t} = \frac{\mathrm{AB}\sin \mathrm{r}}{\mathrm{v}} + \frac{\mathrm{OA}(\sin \mathrm{i} - \sin \mathrm{r})}{\mathrm{v}}$$

Since time taken by each ray, from incident wave front to reflected wave front, must be same

so,

right side of equation must be independent of OA.

This conditions happens only if (sin i-sin r) = 0

Or $\boldsymbol{i = r}$

Thus law of reflection states that angle of incidence i and angle of reflection are always equal.

ALTERNATELY

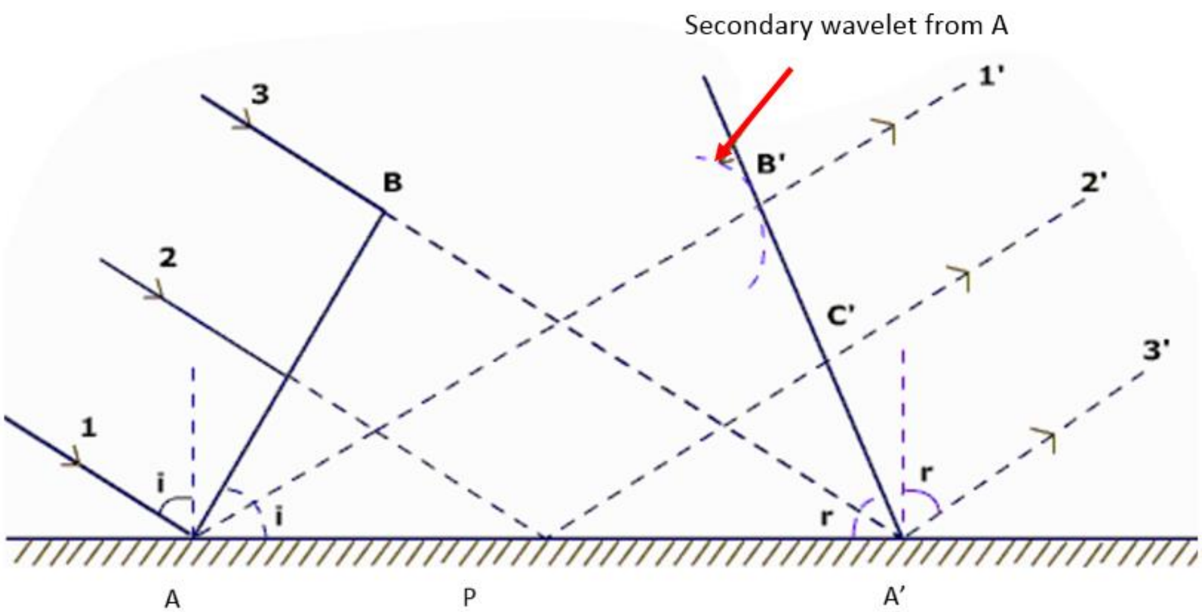
In order to draw a figure to explain the new wavefront position, we can make use of rays along with the wavefront

Remember rays are to show the direction of propagation the light waves, they are perpendicular to the tangent drawn at any point on the wavefront

Rays are easy to draw for a plane wavefront.

1 2 and 3 are incident rays for the incident plane wavefront AB.

The angle of incidence is i for the wave front as well as for the incidents rays.



Note

In case of incident rays, angle of incidence is the angle between the incident ray and the normal at the point of incidence.
For a wavefront it is the angle between the plane wavefront and the surface.

It is easy to visualize this, since the normal is perpendicular to the surface and the ray is perpendicular to the wavefront angle of incidence is the same whether we consider a ray or a wavefront.

We now, consider the triangles A'BA and AB'A'

- side AB'= side BA' as according to Huygens construction secondary wavelets from B and A travel the same distance, both = $v\,\tau$

  v is the velocity of wave, also the velocity of secondary wavelets in the homogeneous medium and τ is the time after which wavelets from point B on the wavefront AB reach A' on surface P

- side AA' is common
- ∠ ABA'= ∠ AB'A' = 90^0 angle between ray and the plane wavefront

The triangles are congruent and therefore, the angles *i* and *r* (as shown in Fig.) would be equal.

Laws of reflection if you recall are

- The angle of reflection is equal to angle of incidence
- The incident ray, reflected ray and the normal at the point of incidence lie in the same plane.

Thus we have used Huygens principle to prove laws of reflection treating light as a wave.

THINK ABOUT THESE

- **Would you explain a spherical wavefront being intercepted by a plane reflecting surface in the same way?**
- **What if the reflecting surface is not plane?**
- **What if the medium is not air around the surface?**
- **What if the medium is heterogeneous (say made of different densities of dissimilar gases)?**

Tips for drawing the diagram

i) To draw the above diagram, bear in mind
ii) Draw the rays first,
iii) Take angle of incidence less than 45^0 or more than 45^0
iv) Draw the incident wave front AB
v) Take BA' as radius and draw a circle with A as center
vi) Draw a tangent to the circular arc from A'
vii) This will be the reflected wavefront.

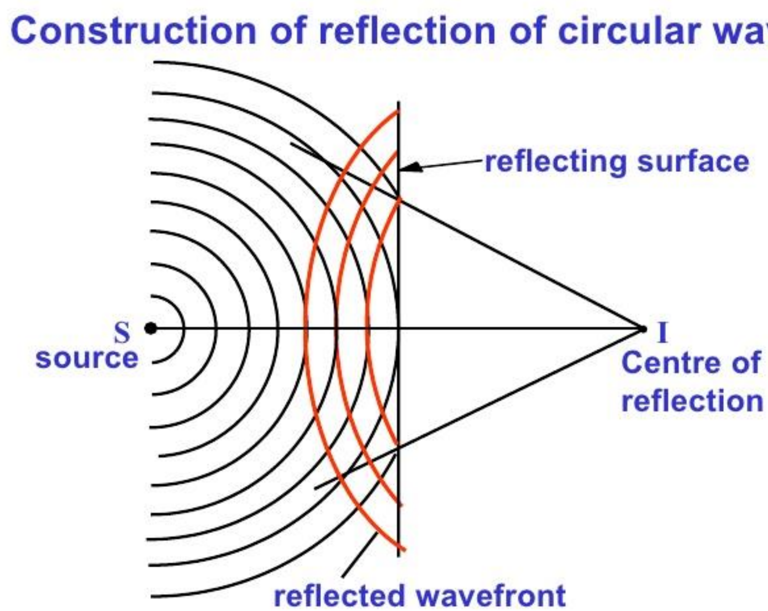
EXAMPLES

Light from a point source is incident on a plane surface.

i) Draw the incident and the reflected wavefront
ii) Explain the location of the image of the source due to reflection.

SOLUTION

i) A point source will emanate spherical wave fronts. We will draw circular wave fronts to represent spherical wavefront in 2 dimension (on a plane sheet of paper)



https://www.slideshare.net/guest73629/s4-e-phy-wavestranverset-presentation

ii) The image is located at the center of reflected wave front, from geometry it would be located as far behind the surface as S in front of the surface.

EXAMPLE

A plane wave front is incident on a curved concave spherical surface (concave mirror)

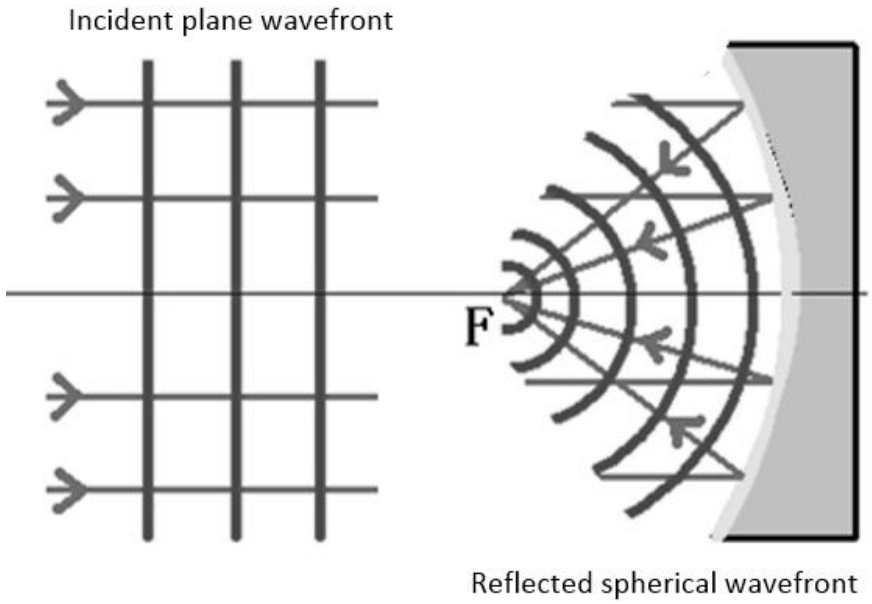
i) Draw the reflected wavefront.

ii) Explain the location of focus in 3 dimensions and 2 dimensions

iii) Draw the reflected wavefront beyond F

SOLUTION

i) Draw the ray diagram then draw the circular wavefront using F as the center, **remember** to keep the separation between wavefront same as for the incident plane wavefront as the velocity /wavelength does not change on reflection



ii) in 3 D the focus would be the center of the spherical reflected wavefront
in 2 D it would be the center of the circular reflected wavefront

iii) Trace the path of the reflected rays beyond F, next complete the concentric circles to show the reflected wavefront beyond F

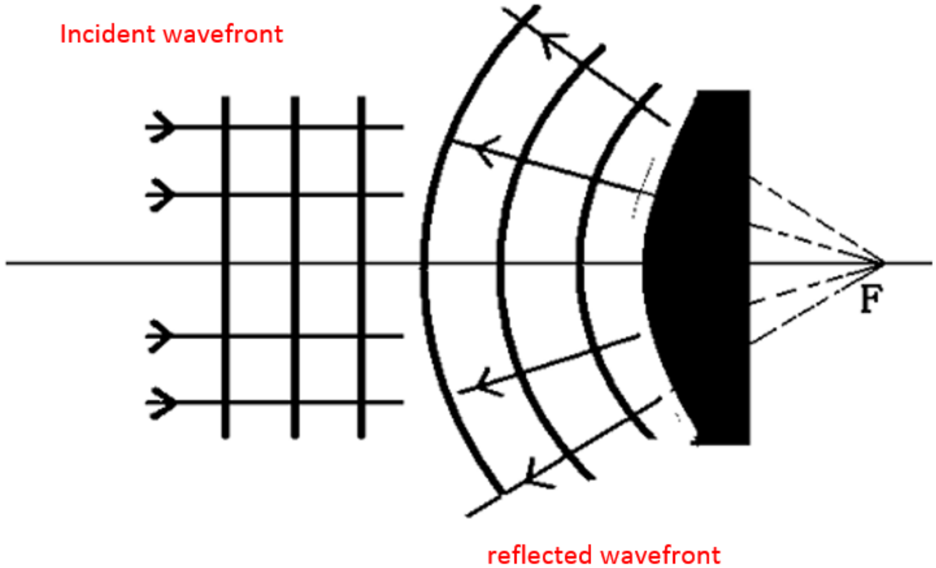
EXAMPLE

A plane wave front is incident on a curved convex spherical surface (convex mirror)

i) Draw the reflected wave front.

ii) Explain the location of focus in 3 dimensions and 2 dimensions

SOLUTION

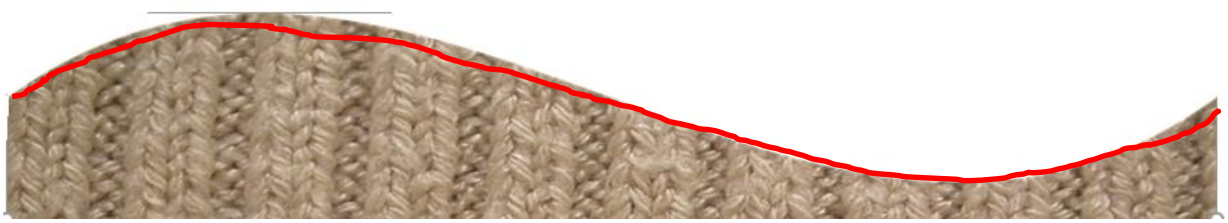


See more

https://www.tes.com/lessons/mvMq1sQNG-7ZEw/reflection-of-wavefronts

TRY THESE

i) a plane wave incident on the following surfaces
ii) a spherical wave incident on the following surfaces



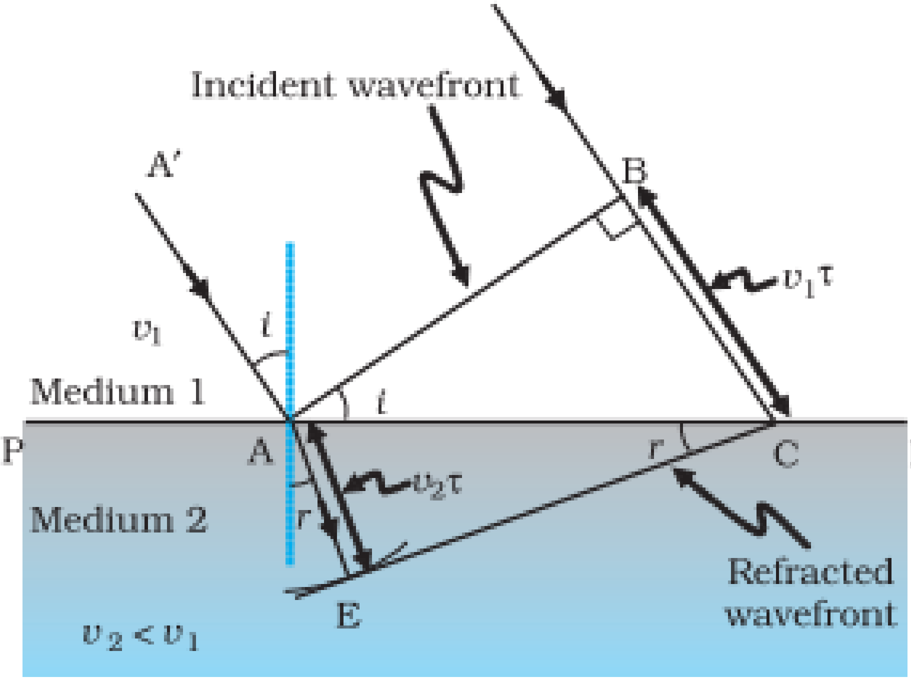
Important to note:
Frequency of reflected wave does not change
Wavelength of the reflected wave does not change
Amplitude changes as some energy may be absorbed by the reflecting surface

8. REFRACTION OF A PLANE WAVE BY PLANE SURFACE

We will now use Huygens principle to derive the laws of refraction

Refraction at a denser medium

Let PP′ represent the surface separating medium 1 and medium 2, as shown in figure.



A plane wave AB is incident at an angle i on the surface PP′ separating medium 1 and medium 2. The plane wave undergoes refraction and CE represents the refracted wavefront. The figure corresponds to $v_2 < v_1$ so that the refracted waves bends towards the normal.

A plane wave AB is incident at an angle i on the surface PP′ separating medium 1 and medium 2.

Medium 1 is rarer as compared to medium 2

The plane wave front AB is incident at an angle i undergoes refraction and CE represents the refracted wave front.

Let v_1 and v_2 ($v_1 > v_2$) represent the speed of light in medium 1 and medium 2, respectively

The figure corresponds to $v_2 < v_1$ so that the refracted waves bends towards the normal.

We assume a plane wave front AB propagating in the direction A′A incident on the interface at an angle of incidence i as shown in the figure.

In oblique incidence as shown, point A of the wave front AB strikes the surface before point B

Let τ be the time taken by the secondary wavelet on the wave front to travel the distance BC in the first medium. Thus, $BC = v_1 \tau$

By this time τ the secondary wave front of radius $v_2\tau$ with A as centre would have travelled forward in second medium whereas the secondary wave front with C as centre would have just started i.e. with zero radius.

In order to determine the shape of the refracted wave front,

we draw a sphere of radius $v_2\tau < v_1\tau$ from the point A as centre in the second medium (the speed of the wave in the second medium is v_2).

Let CE represent a tangent plane drawn from the point C on to the sphere.

Then, AE = $v_2\tau$ and CE would represent the refracted wave front.

If we now consider the triangles ABC and AEC, we obtain

$$\sin i = \frac{BC}{AC} = \frac{v_1\tau}{AC}$$

$$\sin r = \frac{AE}{AC} = \frac{v_2\tau}{AC}$$

where i and *r* are the angles of incidence and refraction, respectively.

Thus we obtain from the above two equations

$$\frac{\sin i}{\sin r} = \frac{v_1}{v_2}$$

From the above equation, we get the important result that if $r < i$ (i.e., if the ray bends toward the normal as $v_1\tau > v_2\tau$),

The speed of the light wave in the second medium (v_2) will be less than the speed of the light wave in the first medium (v_1).

This is in accordance with the wave theory.

Now, if *c* represents the speed of light in vacuum, then,

$$n_1 = \frac{c}{v_1} \quad \text{and} \quad n_2 = \frac{c}{v_2}$$

n_1 or μ_1 *and* n_2 *or* μ_2 are known as the refractive indices of medium 1 and medium 2, respectively.

In terms of the refractive indices, we can write a useful equation

$n_1 \sin i = n_2 \sin r$

This is the ***Snell's law of refraction***.

Further, if λ_1 and λ_2 denote the wavelengths of light in medium 1 and medium 2, respectively and if the distance BC is equal to λ_1 then the distance AE will be equal to λ_2

(Because if the crest from B has reached C in time τ, then the crest from A should have also reached *E* in time τ);

thus,

$$\frac{\lambda_1}{\lambda_2} = \frac{v_1}{v_2}$$

The above equation implies that when a wave gets refracted into a denser medium ($v_1 > v_2$)

- **the wavelength and**
- **the speed of propagation decreases**

but the *frequency* f (= v/λ) remains the same.

Refraction at a rarer medium

We now consider refraction of a plane wave at a rarer medium, i.e**. $v_2 > v_1$.**

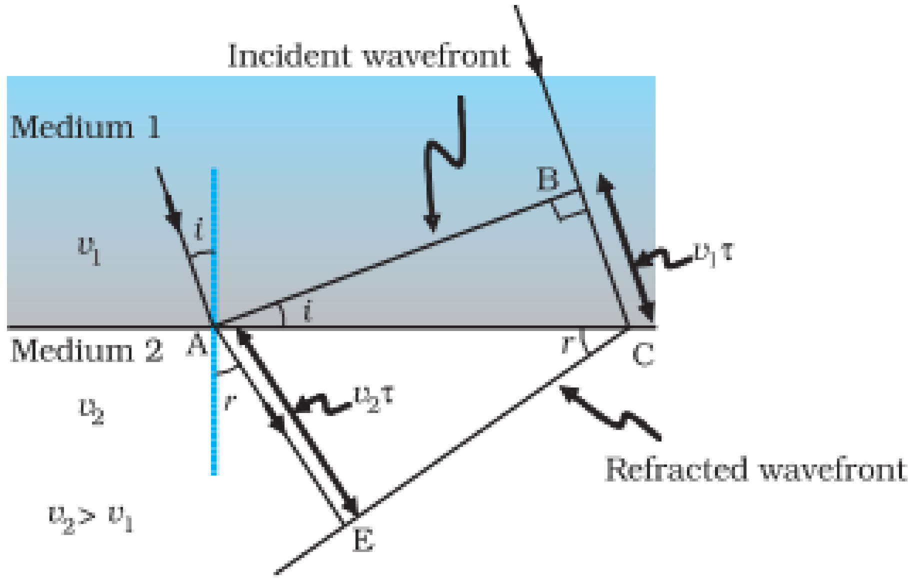
Proceeding in an exactly similar manner, we can construct a refracted wave front as shown in figure.

The angle of refraction *r* will now be greater than angle of incidence *i*. i.e., if the ray bends away from the normal as

$$v_1 \tau < v_2 \tau$$

The speed of the light wave in the second medium (v_2) will be greater than the speed of the light wave in the first medium (v_1).

This is in accordance with the wave theory.



Refraction of a plane wave incident on a rarer medium for which $v_2 > v_1$

The plane wave bends away from the normal.

$$n_1 \sin i = n_2 \sin r$$

The **Snell's law of refraction** still holds in this situation**.**

We define an angle i_c by the following equation

$$\sin i_c = \frac{n_2}{n_1}$$

Thus, if $i = i_C$ then $\sin r = 1$ and $r = 90°$.

Obviously, for $i > i_c$,

There cannot be any refracted wave.

The angle i_c is known as the **critical angle**. For all angles of incidence greater than the critical angle, we will not have any refracted wave and the wave will undergo what is known as **total internal reflection**.

The phenomenon of total internal reflection and its applications have already been discussed

EXAMPLE

When monochromatic light is incident on a surface separating two media, the reflected and refracted light both have the same frequency as the incident frequency. Explain why?

SOLUTION

Reflection and refraction arise through interaction of incident light with the atomic constituents of matter. Atoms may be viewed as oscillators, which take up the frequency of the external agency (light) causing forced oscillations.

The frequency of light emitted by a charged oscillator equals its frequency of oscillation. Thus, the frequency of reflected or refracted light equals the frequency of incident light.

EXAMPLE

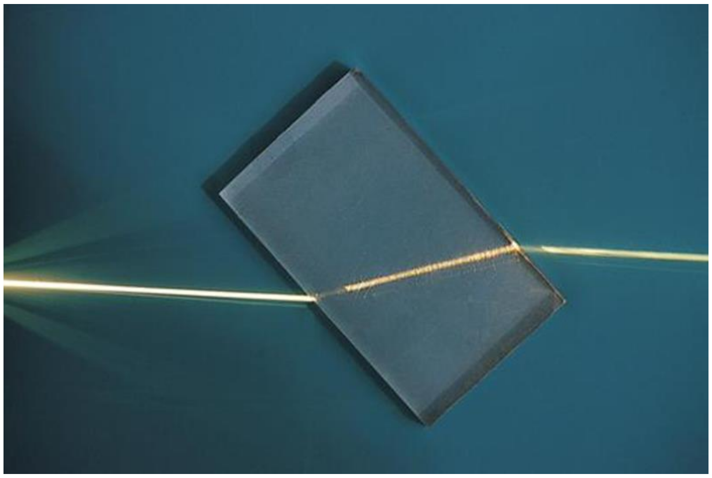
The speed decreases, when light travels from a rarer to a denser medium. Does the reduction in speed imply a reduction in the energy carried by the light wave?

SOLUTION

No. Energy carried by a wave depends on the amplitude of the wave, not on the speed of wave propagation.

TRY THIS

White light is incident on a rectangular glass block



Draw refracted wavefront for red and blue color components when

i) **the ray corresponding to plane wavefront is normal to the surface**
ii) **the ray corresponding to spherical wavefront is normal to the surface**
iii) **plane wavefront is incident obliquely**
iv) **spherical wavefront is incident obliquely**

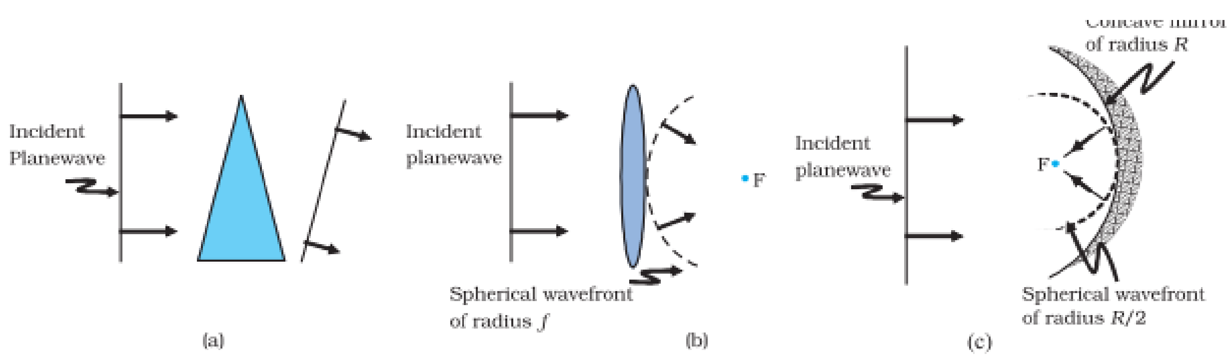
CHANGE IN SHAPE OF WAVE FRONTS

Let us consider a plane wave passing through a thin prism. Since the speed of light waves is less in glass, the lower portion of the incoming wave front (which travels through the greatest thickness of glass) will get delayed resulting in a tilt in the emerging wave front as shown in the figure (a).

In figure (b) we consider a plane wave incident on a thin convex lens; the central part of the incident plane wave traverses the thickest portion of the lens and is delayed the most. The emerging wave front has a depression at the centre and therefore the wave front becomes spherical and converges to the point F which is known as the *focus*.

In figure (c) a plane wave is incident on a concave mirror and on reflection we have a spherical wave converging to the focal point F.

In a similar manner, we can understand refraction and reflection by concave lenses and convex mirrors.



Refraction of a plane wave by (a) a thin prism, (b) a convex lens (c) Reflection of a plane wave by a concave mirror

9. SUMMARY

- Light is an electromagnetic wave
- The Huygens's principle tells us that each point on a wavefront is a source of new secondary waves, which can be used to give the new wavefront at a later time.
- Huygens' construction tells us that the new wavefront is the forward envelope of the secondary waves.
- When the speed of light is independent of direction, the secondary waves are spherical. The rays are then perpendicular to both the wavefront and the time of propagation is the same measured along any ray.
- This principle leads to the well-known laws of reflection and refraction